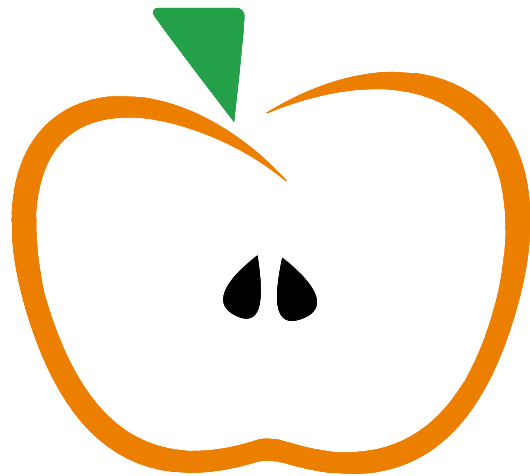




APL Seeds 2023

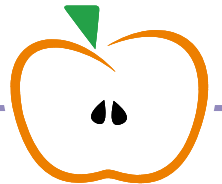
But How Will I Remember
All Those Squiggles?!
— APL Mnemonics

Adám Brudzewsky



Mnemonics

noun A system that helps to remember things.



Lots to remember



More at apl.wiki/typing

$\div N$	Round down to integer
$\lfloor N$	Round up to integer
$\lceil N$	Magnitude (absolute value)
$ N$	e raised to the power N
$*N$	Natural logarithm of N
$\otimes N$	pi times N
$\circ N$	Factorial (Gamma function of N+1)
$!N$	Random number selected from ιJ (when J=0, a real number from $\langle 0,1 \rangle$)
$?J$	Logical Inverse: 0=B
$\sim B$	

DYADIC Syntax	Result
$M+N$	Add N to M
$M-N$	Subtract N from M
$M \times N$	Multiply M and N
$M \div N$	Divide M by N
$M \lceil N$	Residue after dividing N by M
$M * N$	M raised to the power N
$M \otimes N$	Base-M logarithm of N
$M \circ N$	Maximum of M and N
$M \lceil N$	Minimum of M and N
$M \lceil N$	Circular functions ¹

Lots to remember



$\div N$	Round down to integer
$\lfloor N$	Round up to integer
$ N $	Magnitude (absolute value)
e^N	e raised to the power N
$\ln N$	Natural logarithm of N
πN	pi times N
$\Gamma(N+1)$	Factorial (Gamma function of N+1)
rN	Random number selected from rJ (when $J=0$, a real number from $<0,1>$)
$\sim B$	Logical Inverse: $0=B$

DYADIC Syntax	Result
$M+N$	Add N to M
$M-N$	Subtract N from M
$M \times N$	Multiply M and N
$M \div N$	Divide M by N
$M \mid N$	Residue after dividing N by M
M^N	M raised to the power N
$M \log N$	Base-M logarithm of N
$\max(M, N)$	Maximum of M and N
$\min(M, N)$	Minimum of M and N
$\sin M$	Circular functions ¹

Lots to remember



C for
Cap



(intersection)



$\lceil N$

Round up to integer

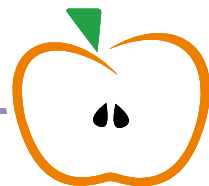


Seiling and wall

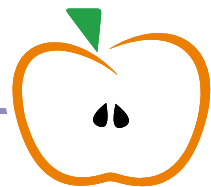
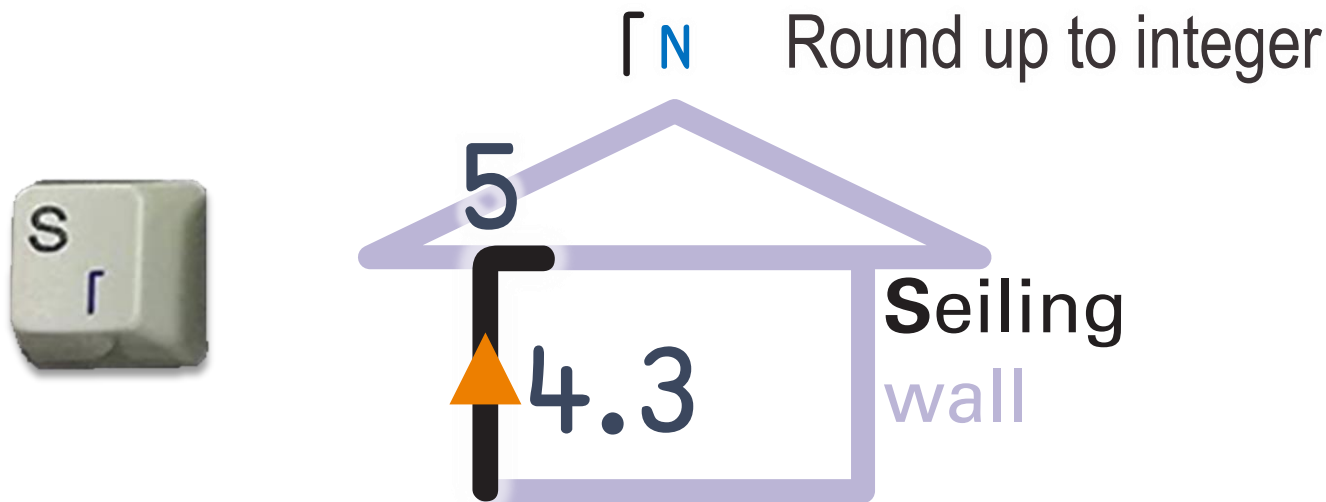
$M \lceil N$

Maximum of M and N

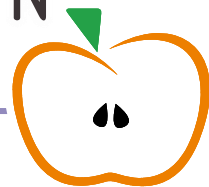
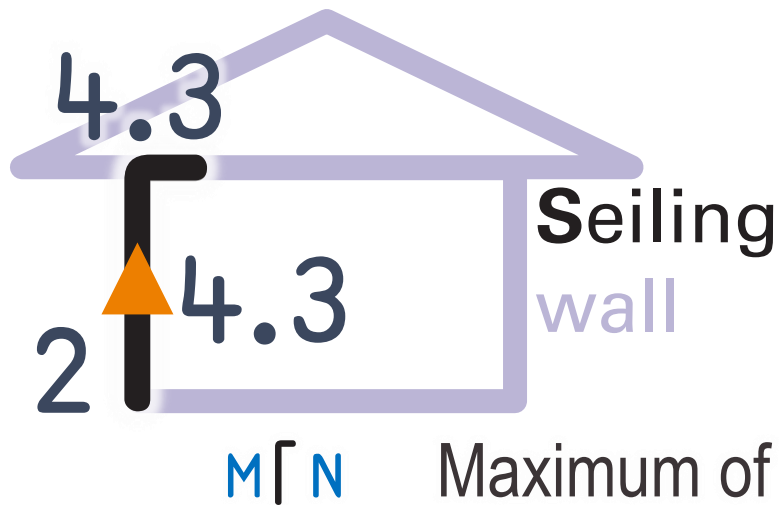
Ceiling
with C



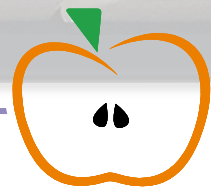
Lots to remember



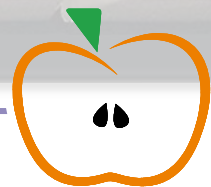
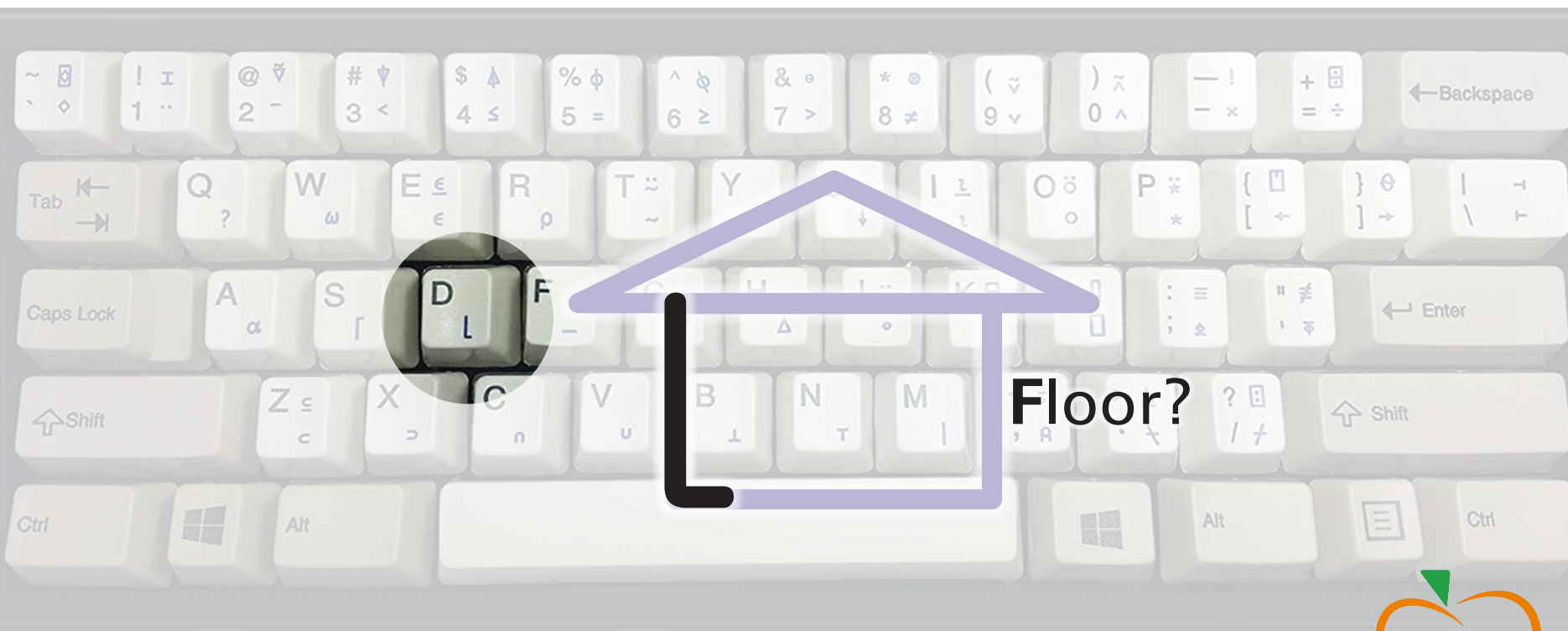
Lots to remember



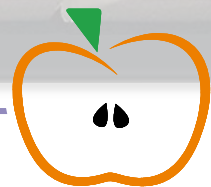
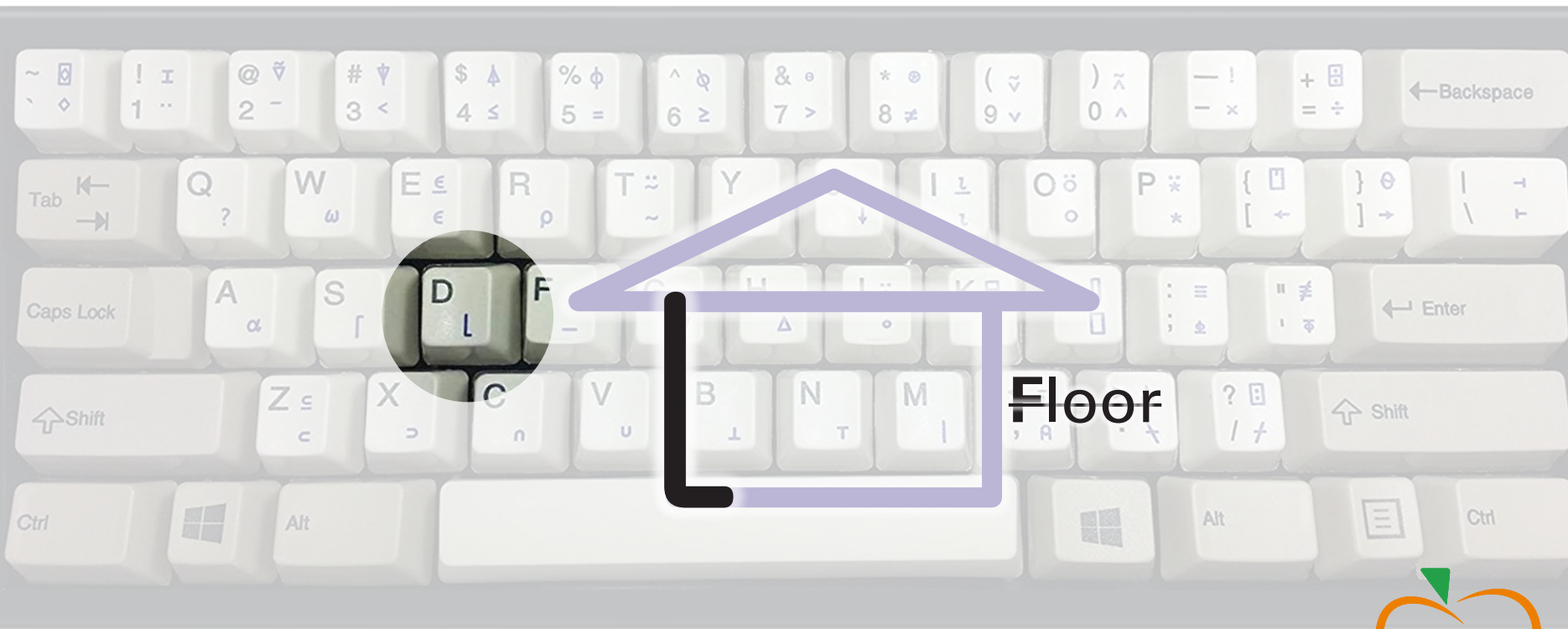
Lots to remember



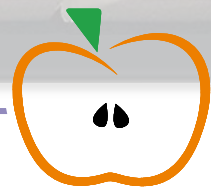
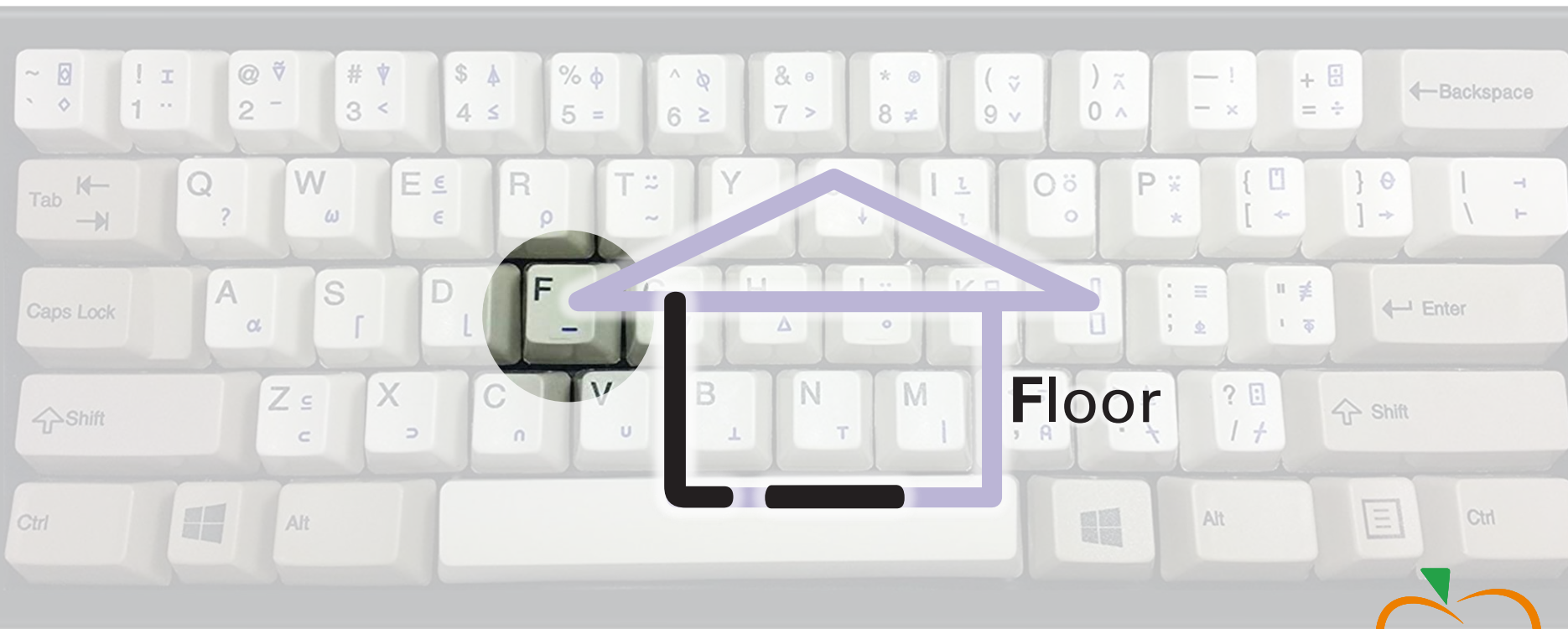
Lots to remember



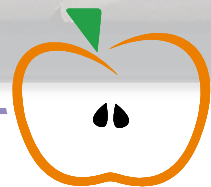
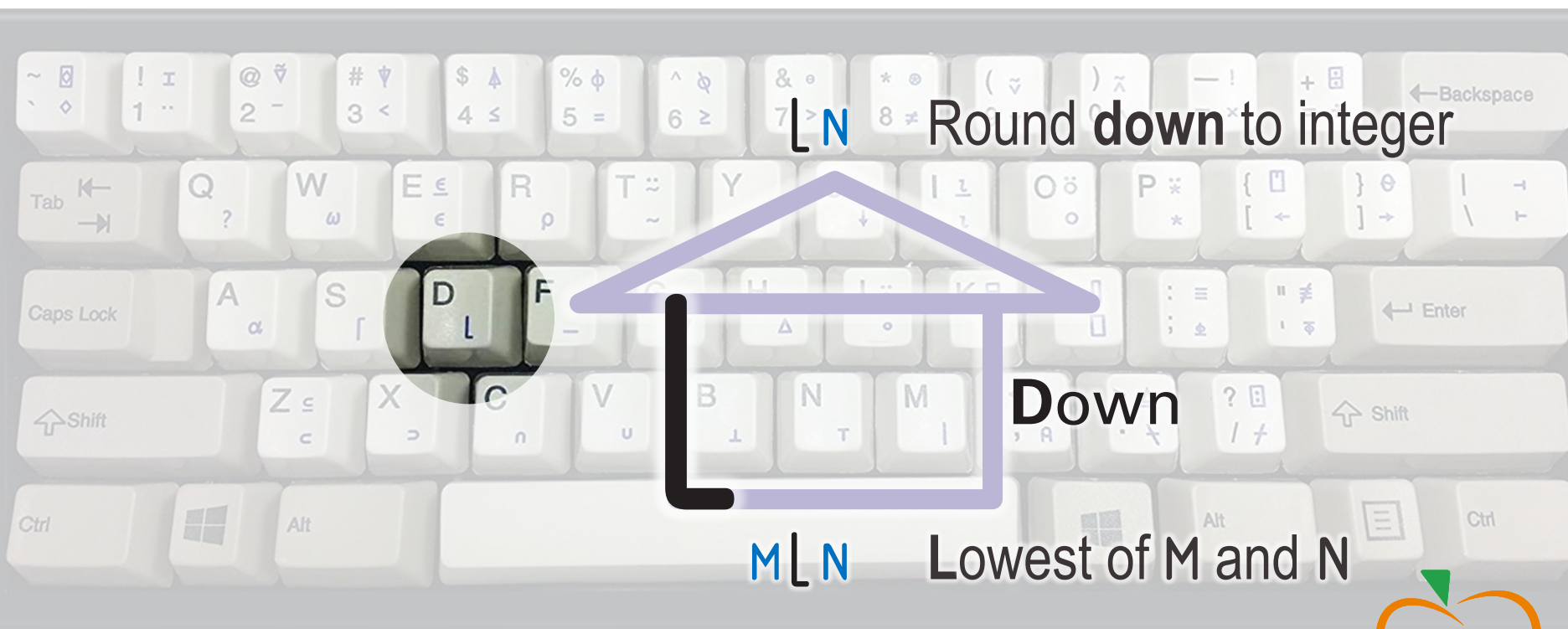
Lots to remember



Lots to remember



Lots to remember

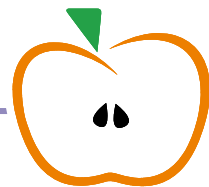


How to remember monad/dyads

Related Concepts

┌ up: ceiling/max

└ down: floor/min



How to remember monad/dyads



Tilde

Related Concepts

┐ up: ceiling/max

└ down: floor/min

~ not: logical/set

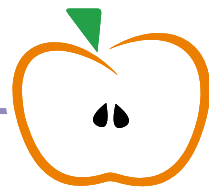
~~stuff~~

"not"

→ ~ 1 0 0 0 1 0
 0 1 1 1 0 1

"but not"

→ 4 1 2 1 5 ~ 5 1
 4 2



How to remember monad/dyads

"shape of"

4 ρ 3 1 2 7

Related Concepts

⌈ up: ceiling/max

⌊ down: floor/min 3 1
2 7

~ not: logical/set

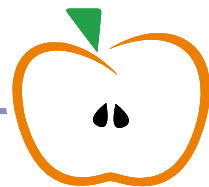
ρ shape: query/change

"reshapes"

2 2 ρ 3 1 2 7



Reshape



How to remember monad/dyads

Default Left Arg.

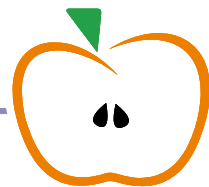
Related Concepts

⌈ up: ceiling/max

⌋ down: floor/min

~ not: logical/set

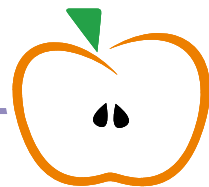
ρ shape: query/change



How to remember monad/dyads

Default Left Arg.

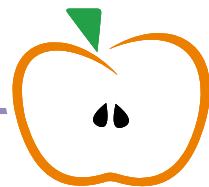
- negate/subtract 3-10
 → -7
 -7
 → -7



How to remember monad/dyads

Default Left Arg.

- negate/subtract 3-10
 → ~~7~~
 -7
 → ~~7~~



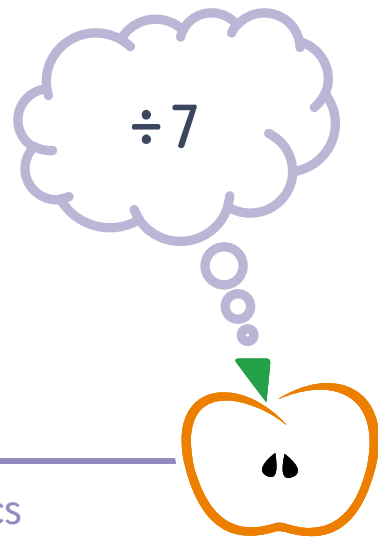
How to remember monad/dyads

Default Left Arg.

- negate/subtract

→ $3-10$
→ -7

→ $0-7$
→ -7



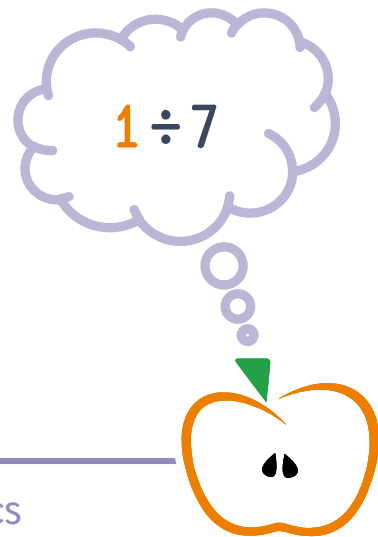
How to remember monad/dyads

Default Left Arg.

- negate/subtract

→ $3-10$
→ -7

→ $0-7$
→ -7



How to remember monad/dyads

Default Left Arg.

– negate/subtract

⊗ (natural) log

→ $10 \otimes 1000$

3

$\otimes 1000$

→ 6.907755279

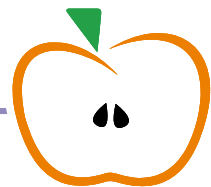
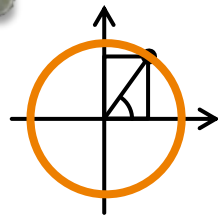
$e \otimes^{-1}$

→ $^{-1}3.141592654$



* Power

∘ Circular



How to remember monad/dyads

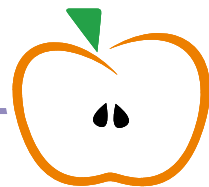
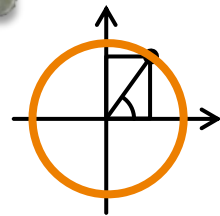
Default Left Arg.

- negate/subtract
- ⊗ (natural) log

logarithm



Power
Circular



How to remember monad/dyads

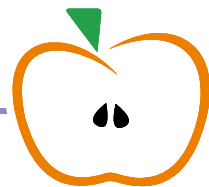
Default Left Arg.

– negate/subtract

⊗ (natural) log

⌵ transpose

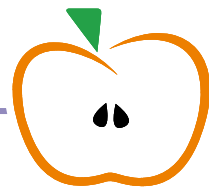
1 2
3 4



How to remember monad/dyads

Default Left Arg.

- negate/subtract
- ⊗ (natural) log
- transpose



How to remember monad/dyads

Default Left Arg.

– negate/subtract

⊗ (natural) log

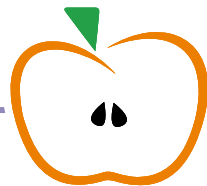
⌵ transpose

1 2

3 4

5 6

7 8



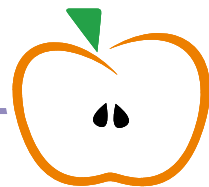
How to remember monad/dyads

Default Left Arg.

- negate/subtract
- ⊗ (natural) log
- ⌵ transpose

1	2
3	4

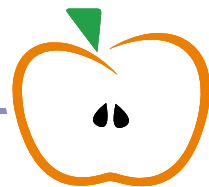
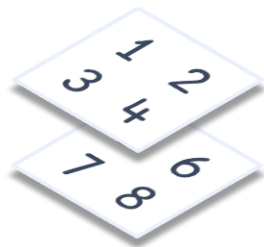
5	6
7	8



How to remember monad/dyads

Default Left Arg.

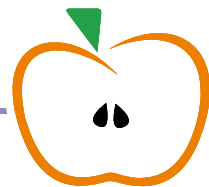
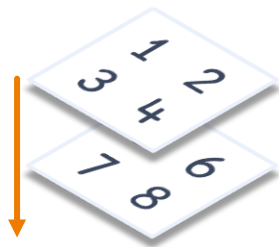
- negate/subtract
- ⊗ (natural) log
- ⌷ transpose



How to remember monad/dyads

Default Left Arg.

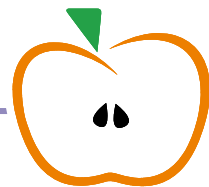
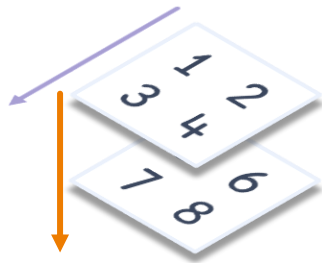
- negate/subtract
- ⊗ (natural) log
- 1⊘ transpose



How to remember monad/dyads

Default Left Arg.

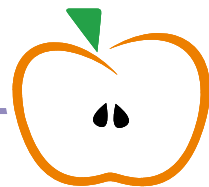
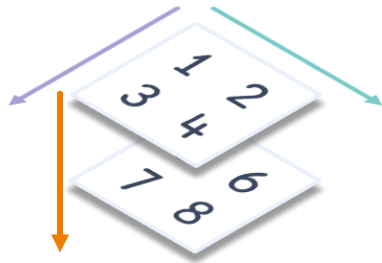
- negate/subtract
- ⊗ (natural) log
- 1 2⊘ transpose



How to remember monad/dyads

Default Left Arg.

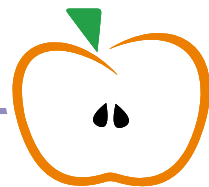
- negate/subtract
- ⊗ (natural) log
- 1 2 3⊘ transpose



How to remember monad/dyads

Default Left Arg.

- negate/subtract
- ⊗ (natural) log
- 1 2 3⊗ transpose



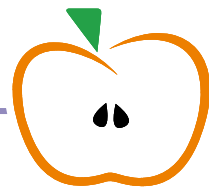
How to remember monad/dyads

Default Left Arg.

– negate/subtract

⊗ (natural) log

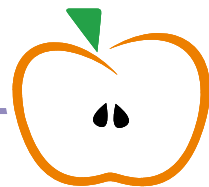
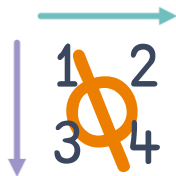
3 2 1⊘ transpose



How to remember glyphs

Default Left Arg.

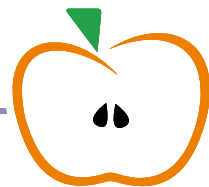
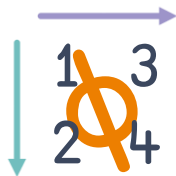
- negate/subtract
- ⊗ (natural) log
- ⌜ transpose



How to remember glyphs

Default Left Arg.

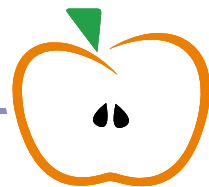
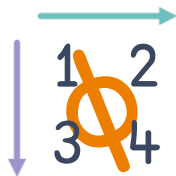
- negate/subtract
- ⊗ (natural) log
- ⌜ transpose



How to remember glyphs

Default Left Arg.

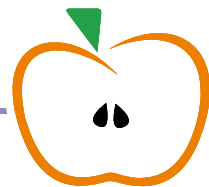
- negate/subtract
- ⊗ (natural) log
- ⌜ transpose



How to remember glyphs

Default Left Arg.

- negate/subtract
- ⊗ (natural) log
- ⌜ transpose



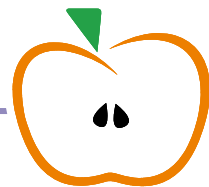
How to remember glyphs

Default Left Arg.

- negate/subtract
- ⊗ (natural) log
- ⌜ transpose



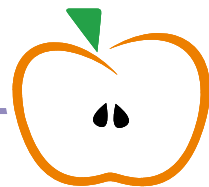
"reverse"



How to remember glyphs

Default Left Arg.

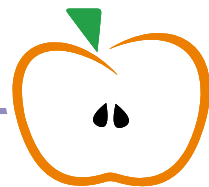
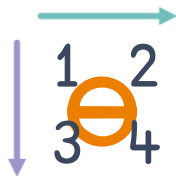
- negate/subtract
- ⊗ (natural) log
- ⌵ transpose



How to remember glyphs

Default Left Arg.

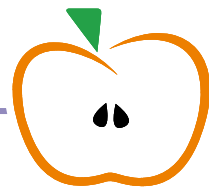
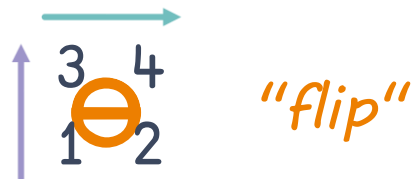
- negate/subtract
- ⊗ (natural) log
- ⌜ transpose



How to remember glyphs

Default Left Arg.

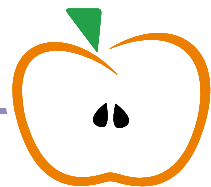
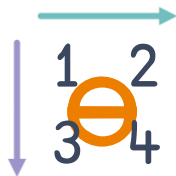
- negate/subtract
- ⊗ (natural) log
- ⌜ transpose



How to remember glyphs

Default Left Arg.

- negate/subtract
- ⊗ (natural) log
- ⌜ transpose



How to remember keyboarding

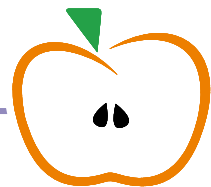


How to remember keyboarding

Default Left Arg.



⌘ transpose

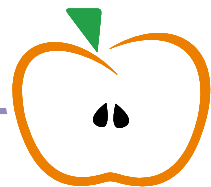


How to remember keyboarding

Default Left Arg.



⌘ transpose

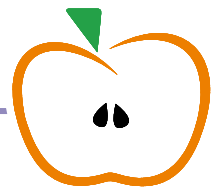


How to remember keyboarding

Default Left Arg.



ϕ transpose

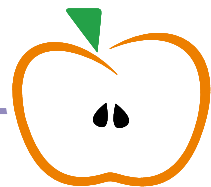


How to remember keyboarding

Default Left Arg.



ϕ transpose

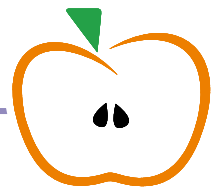


How to remember keyboarding

Default Left Arg.



⌘ transpose



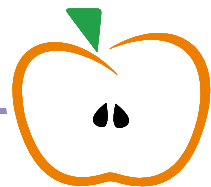
How to remember keyboarding

Default Left Arg.



ϕ transpose

=



How to remember keyboarding

Default Left Arg.

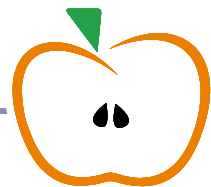


ϕ transpose

\leq

$=$

\geq



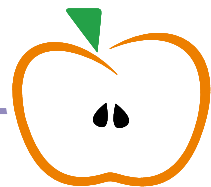
How to remember keyboarding

Default Left Arg.



⌘ transpose

< ≤ = ≥ >



How to remember keyboarding

Default Left Arg.



⌘ transpose

-

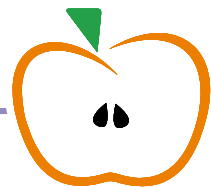
<

≤

=

≥

>



How to remember keyboarding

Default Left Arg.



⌘ transpose

-

<

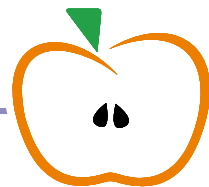
≤

=

≥

>

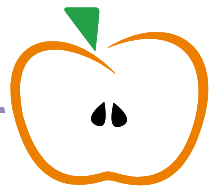
≠



How to remember monad/dyads

Default Left Arg.

- negate/subtract
- ⊗ (natural) log
- ⌷ transpose

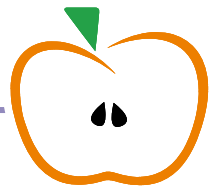


How to remember monad/dyads

Both Fit Glyph

↑ mix/take

↓ split/drop



How to remember monad/dyads

2↑3 1 4 1 5
3 1

take=
Yank!



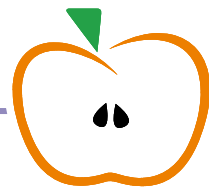
drop=
send to
Under-
world!

2↓3 1 4 1 5
4 1 5

Both Fit Glyph

↑ mix/take

↓ split/drop



How to remember monad/dyads

3 1
2 7

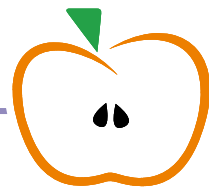
↑ (3 1) (2 7)



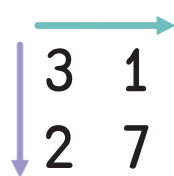
Both Fit Glyph

↑ mix/take

↓ split/drop



How to remember monad/dyads

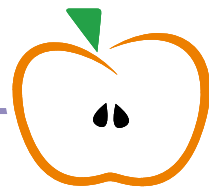
 $\uparrow (3 \ 1) \ (2 \ 7)$



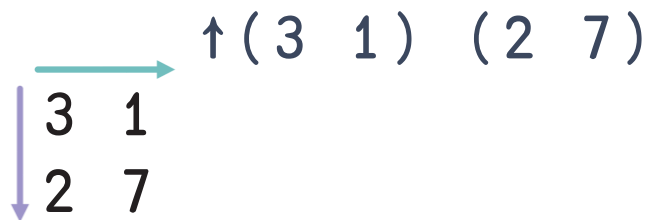
Both Fit Glyph

\uparrow mix/take

\downarrow split/drop



How to remember monad/dyads



Both Fit Glyph

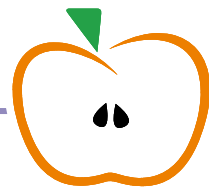
↑ mix/take

↓ split/drop

↓ 2 2ρ3 1 2 7

3	1	2	7
---	---	---	---

*Remember
what ρ does?*



How to remember monad/dyads

$\xrightarrow{\quad} \uparrow (3 \ 1) \ (2 \ 7)$
 $\downarrow \begin{array}{cc} 3 & 1 \\ 2 & 7 \end{array}$



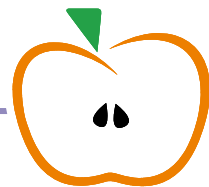
Both Fit Glyph

\uparrow mix/take

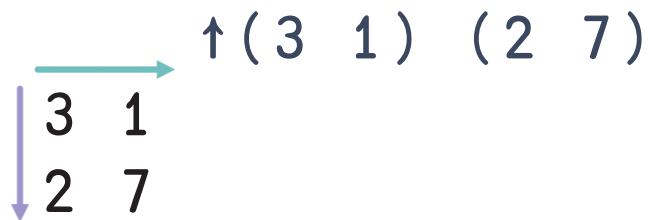
\downarrow split/drop

$\downarrow \xrightarrow{2} 2\rho 3 \ 1 \ 2 \ 7$

3	1	2	7
---	---	---	---



How to remember monad/dyads



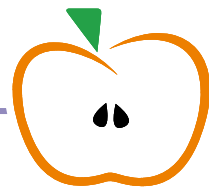
Both Fit Glyph

↑ mix/take

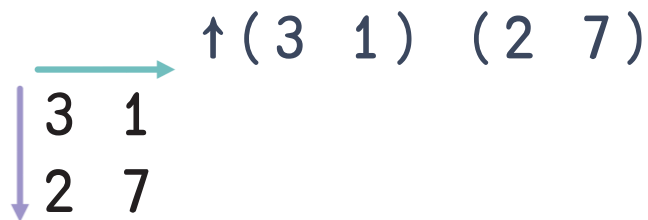
↓ split/drop

↓ 2 → 2 ρ 3 1 2 7

3	1	2	7
---	---	---	---



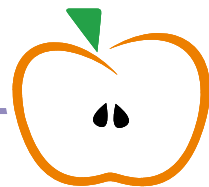
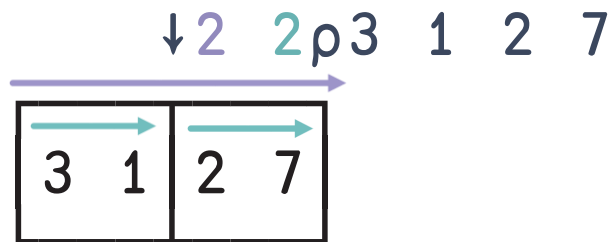
How to remember monad/dyads



Both Fit Glyph

↑ mix/take

↓ split/drop



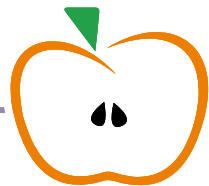
How to remember monad/dyads

Both Fit Glyph

↑ mix/take

↓ split/drop

€ enlist/element



How to remember monad/dyads

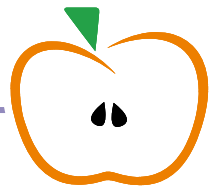
→ € (3 1) (2 7)
 3 1 2 7

Both Fit Glyph

↑ mix/take

↓ split/drop

€ enlist/element



How to remember monad/dyads

→ $\epsilon (3 \ 1) \ (2 \ 7)$
3 1 2 7

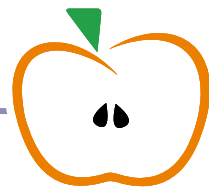
→ $\begin{matrix} 1 & 2 & 3 & 4 & 5 & \epsilon & 3 & 1 & 2 & 7 \\ 1 & 1 & 1 & 0 & 0 & & & & & \end{matrix}$

Both Fit Glyph

↑ mix/take

↓ split/drop

€ enlist/element



How to remember monad/dyads



→ $\epsilon (3 \ 1) \ (2 \ 7)$
 3 1 2 7

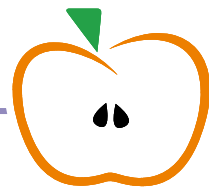
→ 1 2 3 4 5 ϵ 3 1 2 7
 1 1 1 0 0

Both Fit Glyph

↑ mix/take

↓ split/drop

ϵ **enlist/element**



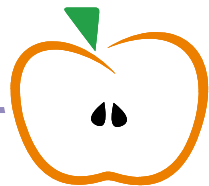
How to remember monad/dyads

Both Fit Glyph

↑ mix/take

↓ split/drop

€ enlist/element



How to remember

Default Left Arg.

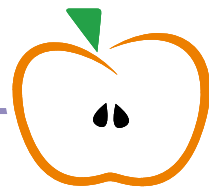
- negate/subtract
- ⊗ (natural) log
- ⌵ transpose

Related Concepts

- ⌈ up: ceiling/max
- ⌊ down: floor/min
- ~ not: logical/set
- ρ shape: query/change

Both Fit Glyph

- ↑ mix/take
- ↓ split/drop
- € enlist/element



What you remember from today

$-Y$ $X-Y$ $\lceil Y$ $X\lceil Y$ $\lfloor Y$ $X\lfloor Y$ $X\cap Y$ ρY $X\rho Y$ $\uparrow Y$ $X\uparrow Y$

$\oplus Y$ $X\oplus Y$ $*Y$ $X*Y$ $\neg N$ $\sim Y$ $X\sim Y$ $\in Y$ $X\in Y$ $\downarrow Y$ $X\downarrow Y$

$\emptyset Y$ $X\emptyset Y$ ϕY ΘY $X<Y$ $X\leq Y$ $X=Y$ $X\geq Y$ $X>Y$ $X\neq Y$

